

ACM/ICPC CheatSheet

Puzzles

Contents

1	STL Useful Tips	2
1.1	Common libraries	2
1.2	I/O	2
1.3	Useful constant	2
1.4	Space waster	3
1.5	Tricks in cmath	3
1.6	Initialize array with predefined value	3
1.7	Modifying sequence operations	3
1.8	Merge	3
1.9	String	4
1.10	Heap	4
1.11	Sort	5
1.12	Permutations	5
1.13	Searching	6
1.14	Random algorithm	6
2	Number Theory	6
2.1	Prime number under 100	6
2.2	Max or min	6
2.3	Greatest common divisor — GCD	6
2.4	Least common multiple — LCM	6
2.5	If prime number	6
2.6	Prime factorization	7
2.7	Leap year	7
2.8	Binary exponential	7
2.9	$a^b \bmod p$	8
2.10	Factorial mod	8
2.11	Generate combinations	8
2.12	10-ary to m -ary	9
2.13	m -ary to 10-ary	9
2.14	Binomial coefficient	9
2.15	Catalan numbers	10
2.16	Eulerian numbers	10
2.17	Karatsuba algorithm in Java	10
2.18	Euler's totient function	11
2.19	Split plane	11
3	Searching Algorithms	11
3.1	Find rank k in array	11
3.2	KMP Algorithm	12
4	Dynamic Programming	13
4.1	0/1 Knapsack problems	13
4.2	Complete Knapsack problems	13
4.3	Longest common subsequence (LCS)	14
4.4	Longest increasing common sequence (LICS)	14
4.5	Longest Increasing Subsequence (LIS)	15
4.6	Maximum submatrix	15
4.7	Partitions of integers	16
4.8	Partitions of sets	17
5	Trees	17
5.1	Tree traversal	17
5.2	Depth and width of tree	18

6 Graph Theory	19
6.1 Graph representation	19
6.2 Flood fill algorithm	21
6.3 SPFA — shortest path	21
6.4 Floyd-Warshall algorithm – shortest path of all pairs	22
6.5 Prim — minimum spanning tree	23
6.6 Eulerian circuit	23
6.7 Topological sort	24

1 STL Useful Tips

1.1 Common libraries

```
/** Functions */
#include<algorithm>
#include<functional> // for hash
#include<climits> // all useful constants
#include<cmath>
#include<cstdio>
#include<cstdlib> // random
#include<ctime>
#include<iostream>
#include<sstream>
#include<iomanip> // right justifying std::right and std::setw(width)
/** Data Structure */
#include<deque> // double ended queue
#include<list>
#include<queue> // including priority_queue
#include<stack>
#include<string>
#include<vector>
```

1.2 I/O

```
// iostream and cstdio are both using I/O streams
// However, they have different behavior,
// pay attention on them if you're using them together.

// cin does not concern with '\n' at end of each line
// however scanf or getline does concern with '\n' at end of each line
// '\n' will be ignored when you use cin to read char.

// when you use getline(cin, str) to read a whole line of input
// please add an extra getline before inputing if previous inputs are numbers
cin >> n;
getline(cin, str) // wasted getline
getline(cin, str) // real input string
```

1.3 Useful constant

```
INT_MIN
INT_MAX
LONG_MIN
LONG_MAX
LLONG_MIN
LLONG_MAX
(~0u) // infinity (for long and long long)
// use (~0u)>>2 for int.
```

1.4 Space waster

```
// consider to redefine data types to void data range problem
#define int long long // make everyone long long
#define double long double // make everyone long double

// function definitions

#undef int // main must return int
int main(void)
#define int long long // redefine int

// rest of program
```

1.5 Tricks in cmath

```
// when the number is too large. use powl instead of pow.
// will provide you more accuracy.
powl(a, b)
(int)round(p, (1.0/n)) // nth root of p
```

1.6 Initialize array with predefined value

```
// for 1d array, use STL fill_n or fill to initialize array
fill(a, a+size_of_a, value)
fill_n(a, size_of_a, value)
// for 2d array, if want to fill in 0 or -1
memset(a, 0, sizeof(a));
// otherwise, use a loop of fill or fill_n through every a[i]
fill(a[i], a[i]+size_of_ai, value) // from 0 to number of row.
```

1.7 Modifying sequence operations

```
void copy(first, last, result);
void swap(a,b);
void swap(first1, last1, first2); // swap range
void replace(first, last, old_value, new_value); // replace in range
void replace_if(first, last, pred, new_value); // replace in conditions
    // pred can be represented in function
    // e.x. bool IsOdd (int i) { return ((i%2)==1); }
void reverse(first, last); // reverse a range of elements
void reverse_copy(first, last, result); // copy a reverse of range of elements
void random_shuffle(first, last); // using built-in random generator to shuffle array
```

1.8 Merge

```
// merge sorted ranges
void merge(first1, last1, first2, last2, result, comp);
// union of two sorted ranges
void set_union(first1, last1, first2, last2, result, comp);
// intersection of two sorted ranges
void set_intersection(first1, last1, first2, last2, result, comp);
```


1.11 Sort

```
void sort(iterator first, iterator last);
void sort(iterator first, iterator last, LessThanFunction comp);
void stable_sort(iterator first, iterator last);
void stable_sort(iterator first, iterator last, LessThanFunction comp);
void partial_sort(iterator first, iterator middle, iterator last);
void partial_sort(iterator first, iterator middle, iterator last, LessThanFunction comp);
bool is_sorted(iterator first, iterator last);
bool is_sorted(iterator first, iterator last, LessThanOrEqualFunction comp);
// example for sort, if have array x, start_index, end_index;
sort(x+start_index, x+end_index);

/** sort a map */
// You cannot directly sort a map<key type, mapped data type>
// if you only want to sort in key type
// you can use insert method to copy map into another map
// b.insert(make_pair(it->first, it->second) /* it is a map iterator */
// this will result a map which sorts key type in increasing order
// if you want to sort key type in decreasing order, then declare your map as
// something like:
// map<char, int, greater<char> >

// if you want to sort based on key, you need to copy the data to a vector
// where elements of vector are pair.
// you can define a PAIR type by using:
typedef pair<char, int> PAIR;

// suppose this is the map
map<char, int> a;

// sort vector in decreasing order
bool cmp_by_value(const PAIR& lhs, const PAIR& rhs) {
    return lhs.second > rhs.second;
}

// sort key in increasing order
bool cmp_by_char(const PAIR& lhs, const PAIR& rhs) {
    return lhs.first < rhs.first;
}

// copy map data to vector
vector<PAIR> b(a.begin(), a.end());

// sort data
sort(b.begin(), b.end(), cmp_by_value);

// you can still call your data by b[i].first and b[i].second.
// THE ABOVE CODES ARE EXAMPLE FOR SORTING A MAP.
// PLEASE USE IT FOR YOUR OWN DEMANDS.
```

1.12 Permutations

```
bool next_permutation(iterator first, iterator last);
bool next_permutation(iterator first, iterator last, LessThanOrEqualFunction comp);
bool prev_permutation(iterator first, iterator last);
bool prev_permutation(iterator first, iterator last, LessThanOrEqualFunction comp);
```

1.13 Searching

```
// will return address of iterator, call result as *iterator;
iterator find(iterator first, iterator last, const T &value);
iterator find_if(iterator first, iterator last, const T &value, TestFunction test);
bool binary_search(iterator first, iterator last, const T &value);
bool binary_search(iterator first, iterator last, const T &value, LessThanOrEqualFunction comp);
```

1.14 Random algorithm

```
rand(time(NULL));
// generate random numbers between [a,b)
rand() % (b - a) + a;
// generate random numbers between [0,b)
rand() % b;
// generate random permutations
random_permutation(anArray, anArray + 10);
random_permutation(aVector, aVector + 10);
```

2 Number Theory

2.1 Prime number under 100

```
// there are 25 numbers
2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37,
41, 43, 47, 53, 59, 61, 67, 71, 73, 79, 83, 89, 97
```

2.2 Max or min

```
int max(int a, int b) { return a>b ? a:b; }
int min(int a, int b) { return a<b ? a:b; }
```

2.3 Greatest common divisor — GCD

```
int gcd(int a, int b)
{
    if (b==0) return a;
    else return gcd(b, a%b);
}
```

2.4 Least common multiple — LCM

```
int lcm(int a, int b)
{
    return a*b/gcd(a,b);
}
```

2.5 If prime number

```
bool prime(int n)
{
    if (n<2) return false;
```

```
if (n<=3) return true;
if (!(n%2) || !(n%3)) return false;
for (int i=5;i*i<=n;i+=6)
    if (!(n%i) || !(n%(i+2))) return false;

return true;
}
```

2.6 Prime factorization

```
// smallest prime factor of a number.
function factor(int n)
{
    int a;
    if (n%2==0)
        return 2;
    for (a=3;a<=sqrt(n);a++)
    {
        if (n%a==0)
            return a;
    }
    return n;
}
```

```
// complete factorization
int r;
while (n>1)
{
    r = factor(n);
    printf("%d", r);
    n /= r;
}
```

2.7 Leap year

```
bool isLeap(int n)
{
    if (n%100==0)
        if (n%400==0) return true;
        else return false;

    if (n%4==0) return true;
    else return false;
}
```

2.8 Binary exponential

```
int binpow (int a, int n)
{
    int res = 1;
    while (n)
    {
        if (n & 1)
        {
            res *= a;
            --n;
        }
    }
}
```

```

    else
    {
        a *= a;
        n >= 1;
    }
    return res;
}

```

2.9 $a^b \bmod p$

```

long powmod(long base, long exp, long modulus) {
    base %= modulus;
    long result = 1;
    while (exp > 0) {
        if (exp & 1) result = (result * base) % modulus;
        base = (base * base) % modulus;
        exp >= 1;
    }
    return result;
}

```

2.10 Factorial mod

```

//n! mod p
int factmod (int n, int p) {
    long long res = 1;
    while (n > 1) {
        res = (res * powmod (p-1, n/p, p)) % p;
        for (int i=2; i<=n%p; ++i)
            res=(res*i) %p;
        n /= p;
    }
    return int (res % p);
}

```

2.11 Generate combinations

```

// n>=m, choose M numbers from 1 to N.
void combination(int n, int m)
{
    if (n<m) return ;
    int a[50]={0};
    int k=0;

    for (int i=1;i<=m;i++) a[i]=i;
    while (true)
    {
        for (int i=1;i<=m;i++)
            cout << a[i] << " ";
        cout << endl;

        k=m;
        while ((k>0) && (n-a[k]==m-k)) k--;
        if (k==0) break;
        a[k]++;
        for (int i=k+1;i<=m;i++)

```

```
    a[i]=a[i-1]+1;
}
}
```

2.12 10-ary to m -ary

```
char a[16]={'0','1','2','3','4','5','6','7','8','9',
'A','B','C','D','E','F'};

string tenToM(int n, int m)
{
    int temp=n;
    string result="";
    while (temp!=0)
    {
        result=a[temp%m]+result;
        temp/=m;
    }

    return result;
}
```

2.13 m -ary to 10-ary

```
string num="0123456789ABCDE";

int mToTen(string n, int m)
{
    int multi=1;
    int result=0;

    for (int i=n.size()-1;i>=0;i--)
    {
        result+=num.find(n[i])*multi;
        multi*=m;
    }

    return result;
}
```

2.14 Binomial coefficient

```
#define MAXN 100 // largest n or m
long binomial_coefficient(n,m) // compute n choose m
int n,m;
{
    int i,j;
    long bc[MAXN][MAXN];
    for (i=0; i<=n; i++) bc[i][0] = 1;
    for (j=0; j<=n; j++) bc[j][j] = 1;
    for (i=1; i<=n; i++)
        for (j=1; j<i; j++)
            bc[i][j] = bc[i-1][j-1] + bc[i-1][j];
    return bc[n][m];
}
```

2.15 Catalan numbers

$$C_n = \sum_{k=0}^{n-1} C_k C_{n-1-k} = \frac{1}{n+1} \binom{n}{k} \quad (1)$$

The first terms of this sequence are 2, 5, 14, 42, 132, 429, 1430 when $C_0 = 1$. This is the number of ways to build a balanced formula from n sets of left and right parentheses. It is also the number of triangulations of a convex polygon, the number of rooted binary trees on $n + 1$ leaves and the number of paths across a lattice which do not rise above the main diagonal.

2.16 Eulerian numbers

$$\binom{n}{k} = k \binom{n-1}{k} + (n-k+1) \binom{n-1}{k-1} \quad (2)$$

```
// This is the number of permutations of length n with exactly k ascending sequences or runs.
// Basis: k=0 has value 1
#define MAXN 100 // largest n or k
long eularian(n,k)
int n,m;
{
    int i,j;
    long e[MAXN][MAXN];
    for (i=0; i<=n; i++) e[i][0] = 1;
    for (j=0; j<=n; j++) e[0][j] = 0;
    for (i=1; i<=n; i++)
        for (j=1; j<i; j++)
            e[i][j] = k*e[i-1][j] + (i-j+1)*e[i-1][j-1];
    return e[n][k];
}
```

2.17 Karatsuba algorithm in Java

```
// fast algorithm to find multiplication of two big numbers.
import java.math.BigInteger;
import java.util.Random;

class Karatsuba {
    private final static BigInteger ZERO = new BigInteger("0");
    public static BigInteger karatsuba(BigInteger x, BigInteger y)
    {
        int N = Math.max(x.bitLength(), y.bitLength());
        if (N <= 2000) return x.multiply(y);
        N=(N/2)+(N %2);
        BigInteger b = x.shiftRight(N);
        BigInteger a = x.subtract(b.shiftLeft(N));
        BigInteger d = y.shiftRight(N);
        BigInteger c = y.subtract(d.shiftLeft(N));
        BigInteger ac = karatsuba(a, c);
        BigInteger bd = karatsuba(b, d);
        BigInteger abcd = karatsuba(a.add(b), c.add(d));
        return ac.add(abcd.subtract(ac).subtract(bd).shiftLeft(N)).add(bd.shiftLeft(2*N));
    }

    public static void main(String[] args)
    {
        long start, stop, elapsed;
        Random random = new Random();
    }
}
```

```

int N = Integer.parseInt(args[0]);
BigInteger a = new BigInteger(N, random);
BigInteger b = new BigInteger(N, random);
start = System.currentTimeMillis();
BigInteger c = karatsuba(a, b);
stop = System.currentTimeMillis();
System.out.println(stop - start);
start = System.currentTimeMillis();
BigInteger d = a.multiply(b);
stop = System.currentTimeMillis();
System.out.println(stop - start);
System.out.println((c.equals(d)));
}
}

```

2.18 Euler's totient function

```

// the positive integers less than or equal to n that are relatively prime to n.
int phi (int n)
{
    int result = n;
    for (int i=2; i*i<=n; ++i)
        if(n %i==0)
    {
        while(n %i==0)
            n /= i;
        result -= result / i;
    }
    if (n > 1)
        result -= result / n;
    return result;
}

```

2.19 Split plane

n lines can split a plane in $\frac{(n+1)n}{2} + 1$ sub-regions.

3 Searching Algorithms

3.1 Find rank k in array

```

int find(int l, int r, int k)
{
    int i=0,j=0,x=0,t=0;

    if (l==r) return a[l];
    x=a[(l+r)/2];
    t=a[x]; a[x]=a[r]; a[r]=t;
    i=l-1;

    for (int j=1; j<=r-1;j++)
        if (a[j]<=a[r])
    {
        i++;
        t=a[i]; a[i]=a[j]; a[j]=t;
    }
    i++;
}

```

```

t=a[i]; a[i]=a[r]; a[r]=t;
if (i==k) return a[i];
if (i<k) return find(i+1, r,k);

return find(l, i-1, k);
}

```

3.2 KMP Algorithm

```

#include <iostream>
#include <string>
#include <vector>

using namespace std;

typedef vector<int> VI;

void buildTable(string& w, VI& t)
{
    t = VI(w.length());
    int i = 0, j = 0;
    t[0] = -1; t[1] = 0;

    while(i < w.length())
    {
        if(w[i-1] == w[j]) { t[i] = j+1; i++; j++; }
        else if(j > 0) j = t[j];
        else { t[i] = 0; i++; }
    }
}

int KMP(string& s, string& w)
{
    int m = 0, i = 0;
    VI t;

    buildTable(w, t);
    while(m+i < s.length())
    {
        if(w[i] == s[m+i])
        {
            i++;
            if(i == w.length()) return m;
        }
        else
        {
            m += i-t[i];
            if(i > 0) i = t[i];
        }
    }
    return s.length();
}

int main(void)
{
    string a = (string) "The example above illustrates the general technique for assembling "+
    "the table with a minimum of fuss. The principle is that of the overall search: "+
    "most of the work was already done in getting to the current position, so very "+

```

```

"little needs to be done in leaving it. The only minor complication is that the "+  

"logic which is correct late in the string erroneously gives non-proper "+  

"substrings at the beginning. This necessitates some initialization code.";  
  

string b = "table";  
  

int p = KMP(a, b);  

cout << p << ":" << a.substr(p, b.length()) << " " << b << endl;  
  

return 0;  

}

```

4 Dynamic Programming

4.1 0/1 Knapsack problems

```

#include<iostream>  
  

using namespace std;  
  

int f[1000]={0};  

int n=0, m=0;  
  

int main(void)
{
    cin >> n >> m;  
  

    for (int i=1;i<=n;i++)
    {
        int price=0, value=0;
        cin >> price >> value;  
  

        for (int j=m;j>=price;j--)
            if (f[j-price]+value>f[j])
                f[j]=f[j-price]+value;
    }
  

    cout << f[m] << endl;  
  

    return 0;
}

```

4.2 Complete Knapsack problems

```

#include<iostream>  
  

using namespace std;  
  

int f[1000]={0};  

int n=0, m=0;  
  

int main(void)
{
    cin >> n >> m;  
  

    for (int i=1;i<=n;i++)
    {

```

```

int price=0, value=0;
cin >> price >> value;

for (int j=price; j<=m; j++)
    if (f[j-price]+value>f[j])
        f[j]=f[j-price]+value;
}

cout << f[m] << endl;

return 0;
}

```

4.3 Longest common subsequence (LCS)

```

int dp[1001][1001];

int lcs(const string &s, const string &t)
{
    int m = s.size(), n = t.size();
    if (m == 0 || n == 0) return 0;
    for (int i=0; i<=m; ++i)
        dp[i][0] = 0;
    for (int j=1; j<=n; ++j)
        dp[0][j] = 0;
    for (int i=0; i<m; ++i)
        for (int j=0; j<n; ++j)
            if (s[i] == t[j])
                dp[i+1][j+1] = dp[i][j]+1;
            else
                dp[i+1][j+1] = max(dp[i+1][j], dp[i][j+1]);
    return dp[m][n];
}

```

4.4 Longest increasing common sequence (LICS)

```

#include<iostream>

using namespace std;

int a[100]={0};
int b[100]={0};
int f[100]={0};
int n=0, m=0;

int main(void)
{
    cin >> n;
    for (int i=1;i<=n;i++) cin >> a[i];
    cin >> m;
    for (int i=1;i<=m;i++) cin >> b[i];

    for (int i=1;i<=n;i++)
    {
        int k=0;
        for (int j=1;j<=m;j++)
        {

```

```

        if (a[i]>b[j] && f[j]>k) k=f[j];
    else if (a[i]==b[j] && k+1>f[j]) f[j]=k+1;
}
}

int ans=0;
for (int i=1;i<=m;i++)
if (f[i]>ans) ans=f[i];

cout << ans << endl;

return 0;
}

```

4.5 Longest Increasing Subsequence (LIS)

```

#include<iostream>

using namespace std;

int n=0;
int a[100]={0}, f[100]={0}, x[100]={0};

int main(void)
{
    cin >> n;
    for (int i=1;i<=n;i++)
    {
        cin >> a[i];
        x[i]=INT_MAX;
    }

    f[0]=0;

    int ans=0;
    for(int i=1;i<=n;i++)
    {
        int l=0, r=i;

        while (l+1<r)
        {
            int m=(l+r)/2;
            if (x[m]<a[i]) l=m; else r=m;
            // change to x[m]<=a[i] for non-decreasing case
        }

        f[i]=l+1;
        x[l+1]=a[i];
        if (f[i]>ans) ans=f[i];
    }

    cout << ans << endl;

    return 0;
}

```

4.6 Maximum submatrix

```

// URAL 1146 Maximum Sum
#include<iostream>

using namespace std;

int a[150][150]={0};
int c[200]={0};

int maxarray(int n)
{
    int b=0, sum=-100000000;
    for (int i=1;i<=n;i++)
    {
        if (b>0) b+=c[i];
        else b=c[i];
        if (b>sum) sum=b;
    }

    return sum;
}

int maxmatrix(int n)
{
    int sum=-100000000, max=0;

    for (int i=1;i<=n;i++)
    {
        for (int j=1;j<=n;j++)
            c[j]=0;

        for (int j=i;j<=n;j++)
        {
            for (int k=1;k<=n;k++)
                c[k]+=a[j][k];
            max=maxarray(n);
            if (max>sum) sum=max;
        }
    }

    return sum;
}

int main(void)
{
    int n=0;
    cin >> n;
    for (int i=1;i<=n;i++)
        for (int j=1;j<=n;j++)
            cin >> a[i][j];

    cout << maxmatrix(n);
    return 0;
}

```

4.7 Partitions of integers

```

#define MAXN 100 // largest n or m
long int_coefficient(n,k) // compute f(n,k)

```

```

int n,m;
{
    int i,j;
    long f[[MAXN][MAXN];
    f[1][1] = 1;
    for (i=0;i<=n;i++) f[i][0] = 0;
    for (i=1; i<=n; i++)
        for (j=1; j<i; j++)
            if (i-j <= 0)
                f[i][j] = f[i][k-1];
            else
                f[i][j] = f[i-j][k]+f[i][k-1];
    return f[n][k];
}

```

4.8 Partitions of sets

Number of ways to partition $n + 1$ items into k sets.

$$\binom{n}{k} = k \binom{n-1}{k} + \binom{n-1}{k-1} \quad (3)$$

where

$$\binom{n}{1} = \binom{n}{n} = 1 \quad (4)$$

5 Trees

5.1 Tree traversal

```

int L[100]={0};
int R[100]={0};

void DLR(int m)
{
    cout << m << " ";
    if (L[m]!=0) DLR(L[m]);
    if (R[m]!=0) DLR(R[m]);
}

void LDR(int m)
{
    if (L[m]!=0) LDR(L[m]);
    cout << m << " ";
    if (R[m]!=0) LDR(R[m]);
}

void LRD(int m)
{
    if (L[m]!=0) LRD(L[m]);
    if (R[m]!=0) LRD(R[m]);
    cout << m << " ";
}

int main(void)
{
    cin >> n;
    for (int i=1;i<=n;i++)
        cin >> L[i] >> R[i];
}

```

```

DLR(1); cout << endl;
LDR(1); cout << endl;
LRD(1); cout << endl;

return 0;
}

```

5.2 Depth and width of tree

```

#include <iostream>
#include <queue>
#include <stack>

using namespace std;

int l[100]={0};
int r[100]={0};
stack<int> mystack;
int n=0;
int w=0;
int d=0;

int depth(int n)
{
    if (l[n]==0 && r[n]==0)
        return 1;

    int depthl=depth(l[n]);
    int depthr=depth(r[n]);
    int dep=depthl>depthr ? depthl:depthr;
    return dep+1;
}

void width(int n)
{
    if (n>=d)
    {
        int t=0,x;
        stack<int> tmpstack;
        while (!mystack.empty())
        {
            x=mystack.top();
            mystack.pop();
            if (x!=0)
            {
                t++;
                tmpstack.push(l[x]);
                tmpstack.push(r[x]);
            }
        }
        w=w>t?w:t;
        mystack=tmpstack;
        width(n+1);
    }
}

```

```

int main(void)
{
    cin >> n;

    for (int i=1;i<=n;i++)
        cin >> l[i] >> r[i];

    d=depth(1);
    mystack.push(1);
    width(1);

    cout << w << " " << d << endl;

    return 0;
}

```

6 Graph Theory

6.1 Graph representation

```

// The most common way to define graph is to use adjacency matrix
// example:
//      (1) (2) (3) (4) (5)
// (1)  2   0   5   0   0
// (2)  4   2   0   0   1
// (3)  3   0   0   1   4
// (4)  6   9   0   0   0
// (5)  1   1   1   1   5
// it's always a square matrix.
// suppose a graph has n nodes, if given exactly adjacency matrix
for (int i=1;i<=n;i++)
    for (int j=1;j<=n;j++)
    {
        cin << a[i][j] << endl;
    }
// Usually will go like this representation in data
// start_node end_node weight
// suppose m lines
for (int i=1;i<=m;i++)
{
    int x=0, y=0, t=0;
    cin >> x >> y >> t;
    a[x][y]=t;
    // if undirected graph
    a[y][x]=t;
}
// another variant: on the ith line, has data as
// end_node weight
// when you read data, you can assign matrix as
a[i][x]=t;
// if undirected graph
a[x][i]=t;

// Initialization of graph !!!IMPORTANT
// Depends on usage, normally initialize as 0 for all elements in matrix.
// so that 0 means no connection, non-0 means connection
// (for problem without weight, use weight as 1)
// If weights are important in this context (especially searching for path)

```

```

// Initialize graph as infinity for all elements in matrix.

// Another way to store graph is Adjacency list
// No space advantage if using array (unknown maximum number for in-degree).
// Big space advantage if using dynamic data structure (like list, vector).
// each row represent a node and its connectivity.
// we don't need it so much due to it's search efficiency.
// let's define a node as
struct Node{
    int id; // node id
    int w; // weight
};

// suppose n nodes and m lines of inputs as
// start_node end_node weight
// assume using <vector> in this example
// g is a vector, and each element of g is also a vector of Node
for (int i=1;i<=m;i++)
{
    int x=0, y=0, t=0;
    cin >> x >> y >> t;
    Node temp; temp.id=y; temp.w=t;
    g[x].push_back(temp);
    // if undirected
    temp.id=x;
    g[y].push_back(temp);
}
// Note that you don't need this node structure if graph has only connectivity information.

***** Special Structure *****

// Special structure here is usually not a typical graph, like city-blocks, triangles
// They are represented in 2-d array and shows weights on nodes instead of edges.
// Note that in this case travel through edge has no cost, but visit node has cost.

// Triangles: Read data like this
// 1
// 1 2
// 4 2 7
// 7 3 1 5
// 6 2 9 4 6
for (int i=1;i<=n;i++)
    for (int j=i;j<=n;j++)
        cin >> a[i][j];

// Simple city-blocks: it's just like first form of adjacency matrix, but this time
// represents weights on nodes, may not be square matrix.
// 1 2 4 5 6
// 2 4 5 1 3
// 4 5 2 3 6
for (int i=1;i<=n;i++)
    for (int j=1;j<=m;j++)
        cin >> a[i][j];

// More complex data structures: typical city-block structure may has some constraints on
// questions, but it has no boundaries. However, some questions requires to form a maze.
// In these cases, data structures can be very flexible, it totally depends on how the question
// presents the data. A usual way is to record it's adjacent blocks information:
struct Block{
    bool l[4]; // if has 8 neighbors then use bool l[8];

```

```

    // label them as your favor, e.x.
    //   1   1 2 3
    // 4 x 2 8 x 4
    //   3   7 6 5
    // true if there is path, false if there is boundary
// other informations (optional)
int weight;
int component_id;
// etc.
};

// Note that usually we use array from index 1 instead of 0 because sometimes
// you need index 0 as your boundary, and start from index 1 will give you
// advantage on locating nodes or positions

```

6.2 Flood fill algorithm

```

//component(i) denotes the
//component that node i is in
void flood_fill(new_component)
do
    num_visited = 0
    for all nodes i
        if component(i) = -2
            num_visited = num_visited + 1
            component(i) = new_component

    for all neighbors j of node i
        if component(j) = nil
            component(j) = -2
until num_visited = 0

void find_components()
num_components = 0
for all nodes i
    component(node i) = nil
for all nodes i
    if component(node i) is nil
        num_components = num_components + 1
        component(i) = -2
        flood_fill(component num_components)

```

6.3 SPFA — shortest path

```

int q[3001]={0}; // queue for node
int d[1001]; // record shortest path from start to ith node
bool f[1001];
int a[1001][1001]={0}; // adjacency list
int w[1001][1001]={0}; // adjacency matrix

int main(void)
{
    int n=0, m=0;
    cin >> n >> m;

    for (int i=1;i<=m;i++)
    {

```

```

int x=0, y=0, z=0;
cin >> x >> y >> z; // node x to node y has weight z
a[x][0]++;
a[x][a[x][0]]=y;
w[x][y]=z;
/*
// for undirected graph
a[x][0]++;
a[y][a[y][0]]=x;
w[y][x]=z;
*/
}
}

int s=0, e=0;
cin >> s >> e; // s: start, e: end
SPFA(s);
cout << d[e] << endl;

return 0;
}

void SPFA(int v0)
{
    int t,h,u,v;
    for (int i=0;i<1001;i++) d[i]=INT_MAX;
    for (int i=0;i<1001;i++) f[i]=false;
    d[v0]=0;
    h=0; t=1; q[1]=v0; f[v0]=true;

    while (h!=t)
    {
        h++;
        if (h>3000) h=1;
        u=q[h];
        for (int j=1; j<=a[u][0];j++)
        {
            v=a[u][j];
            if (d[u]+w[u][v]<d[v]) // change to > if calculating longest path
            {
                d[v]=d[u]+w[u][v];
                if (!f[v])
                {
                    t++;
                    if (t>3000) t=1;
                    q[t]=v;
                    f[v]=true;
                }
            }
        }
        f[u]=false;
    }
}

```

6.4 Floyd-Warshall algorithm – shortest path of all pairs

```

// map[i][j]=infinity at start
void floyd()
{

```

```

for (int k=1; k<=n; k++)
    for (int i=1; i<=n; i++)
        for (int j=1; j<=n; j++)
            if (i!=j && j!=k && i!=k)
                if (map[i][k]+map[k][j]<map[i][j])
                    map[i][j]=map[i][k]+map[k][j];
}

```

6.5 Prim — minimum spanning tree

```

int d[1001]={0};
bool v[1001]={0};
int a[1001][1001]={0};

int main(void)
{
    int n=0;
    cin >> n;
    for (int i=1;i<=n;i++)
    {
        int x=0, y=0, z=0;
        cin >> x >> y >> z;
        a[x][y]=z;
    }
    for (int i=1;i<=n;i++)
        for (int j=1;j<=n;j++)
            if (a[i][j]==0) a[i][j]=INT_MAX;

    cout << prim(1,n) << endl;
}
int prim(int u, int n)
{
    int mst=0,k;

    for (int i=0;i<d.length;i++) d[i]=INT_MAX;
    for (int i=0;i<v.length;i++) v[i]=false;

    d[u]=0;
    int i=u;

    while (i!=0)
    {
        v[i]=true;k=0;
        mst+=d[i];
        for (int j=1;j<=n;j++)
            if (!v[j])
            {
                if (a[i][j]<d[j]) d[j]=a[i][j];
                if (d[j]<d[k]) k=j;
            }
        i=k;
    }
    return mst;
}

```

6.6 Eulerian circuit

```

// USACO Fence
#include<iostream>

using namespace std;

int f[100]={0}, ans[100]={0};
bool g[100][100]={0}, v[100]={0};
int n=0, m=0, c=0;

void dfs(int k)
{
    for (int i=1;i<=n;i++)
        if (g[k][i])
        {
            g[k][i]=false;
            g[i][k]=false;
            dfs(i);
        }
    m++;
    ans[m]=k;
}

int main(void)
{
    cin >> n >> m;

    for (int i=1;i<=m;i++)
    {
        int x=0, y=0;
        g[x][y]=true;
        g[y][x]=true;
        f[x]++;
        f[y]++;
    }

    m=0;
    int k1=0;
    for (int i=1;i<=n;i++)
    {
        if (f[i]%2==1) k1++;
        if (k1>2)
        {
            cout << "error" << endl;
            return 0;
        }
        if (f[i]%2 && c==0) c=i;
    }

    if (c==0) c=1;
    dfs(x);

    for (int i=m;i>=1;i--) cout << ans[i] << endl;
    return 0;
}

```

6.7 Topological sort

```

// Find any solution of topological sort.
#include<iostream>

using namespace std;

int f[100]={0}, ans[100]={0};
bool g[100][100]={0}, v[100]={0};
int n=0, m=0;

void dfs(int k)
{
    int i=0;
    v[k]=true;
    for (int i=1;i<=n;i++)
        if (g[k][i] && !v[i]) dfs(i);

    m++;
    ans[m]=k;
}

int main(void)
{
    cin >> n >> m;

    for (int i=1;i<=m;i++)
    {
        int x=0, y=0;
        cin >> x >> y;
        g[y][x]=true;
    }

    m=0;
    for (int i=1;i<=n;i++)
        if (!v[i]) dfs(i);

    for (int i=1;i<=n;i++) cout << ans[i] << endl;
    return 0;
}

```

```

// Find the order of topological sort is dictionary minimum
#include<iostream>
```

```

using namespace std;

int f[100]={0}, ans[100]={0};
bool g[100][100]={0}, v[100]={0};
int n=0, m=0;

int main(void)
{
    cin >> n >> m;

    for (int i=1;i<=m;i++)
    {
        int x=0, y=0;
        cin >> x >> y;
        g[x][y]=true;
        f[y]++;
    }

    for (int i=0;i<=m;i++)
        if (!v[i]) dfs(i);
}
```

```
for (int i=1;i<=n;i++)
{
    for (int j=1;j<=n;j++)
    {
        if (f[j]==0 && !v[j]) break;

        if (f[j]!=0)
        {
            cout << "error" << endl;
            return 0;
        }

        ans[i]=j;
        v[j]=true;
        for (int k=1;k<=n;k++)
            if (g[j][k]) f[k]--;
    }
}
for (int i=1;i<=n;i++) cout << ans[i] << endl;
return 0;
}
```
